

FUNDAMENTAL ELECTRONIC CIRCUITS

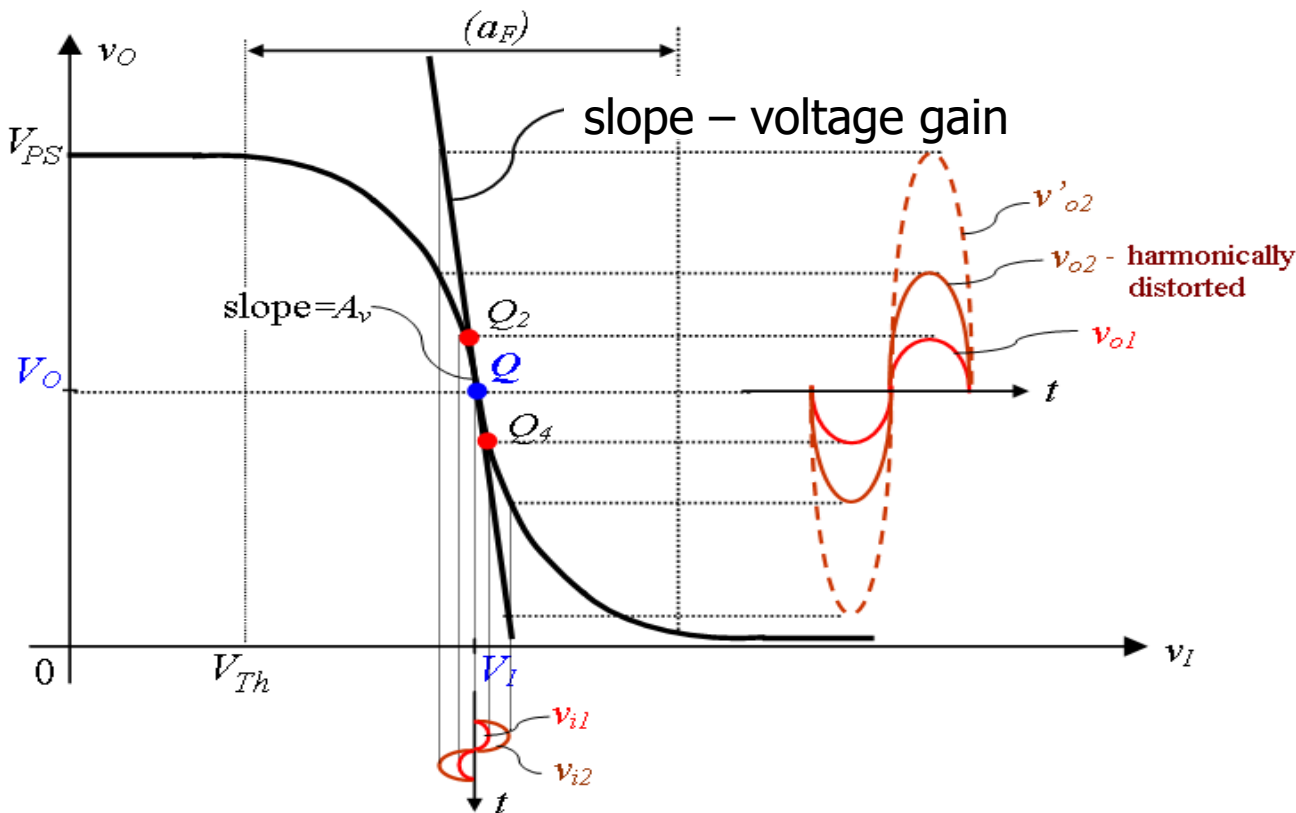
Assist. prof. Laura-Nicoleta IVANCIU, Ph.D.

C3 – MOSFET basic amplifiers

Contents

- MOSFET small-signal model
- MOSFET basic amplifiers

➤ Small-signal motivation - revisited

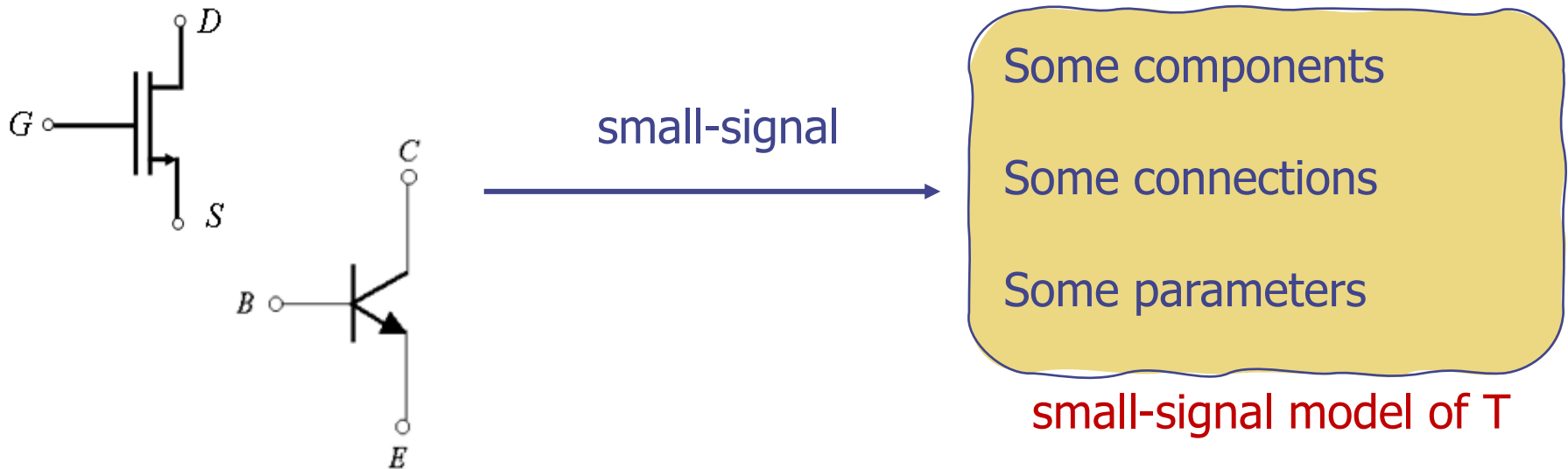


Small-signal model
(linear model)
needed to compute

Voltage gain: $A_v = \frac{v_o}{v_i}$

Small-signal model is valid in the **narrow linear region around Q** .

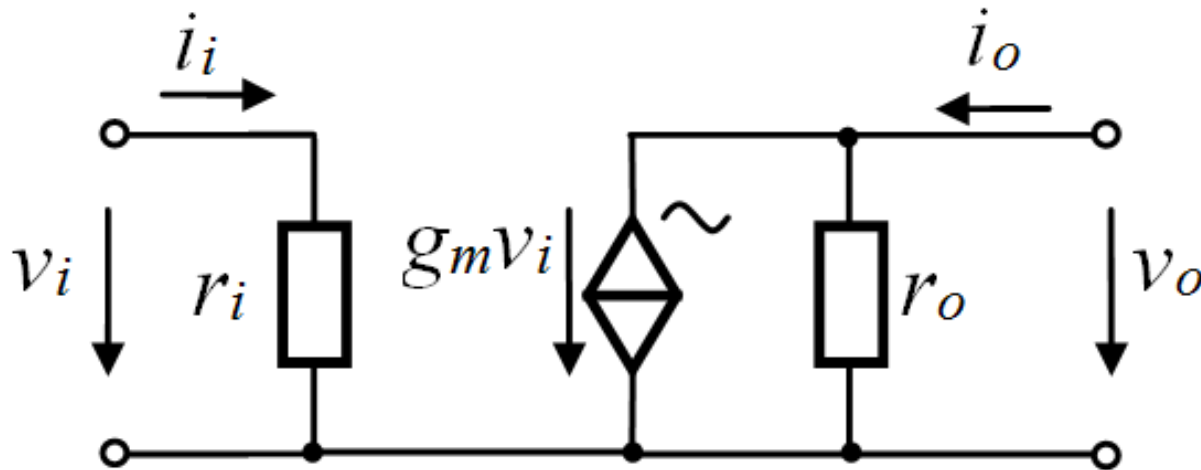
➤ Small-signal operation - intro



Hints:

- keep names of terminals
- use voltage-controlled current source
- values of parameters are computed in $Q(V_{DS}; I_D)$ or $Q(V_{CE}; I_C)$

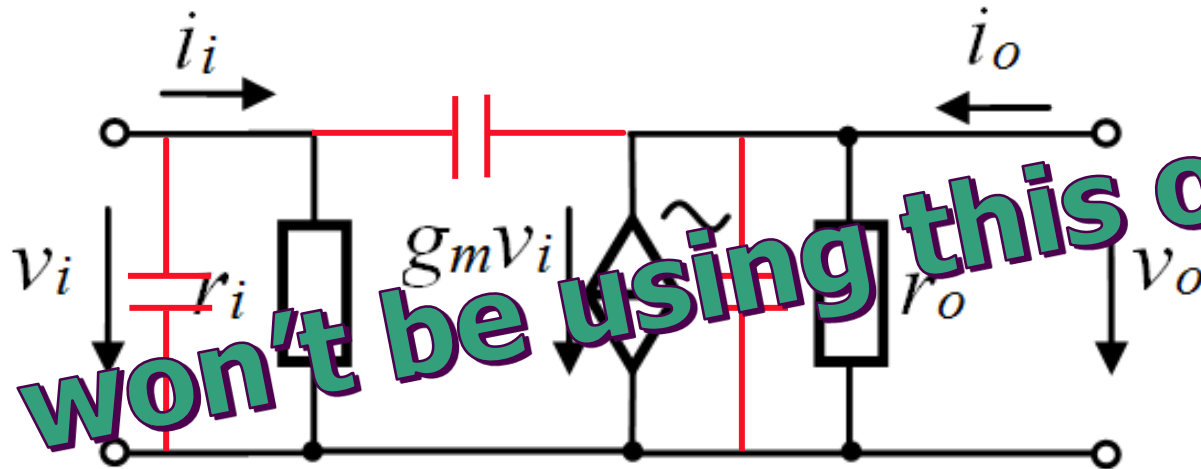
➤ Small-signal model – low & medium frequency



• **two-port network**

- ✓ input resistance: r_i
- ✓ transfer: voltage-controlled current source: $g_m v_i$
- ✓ output resistance: r_o

- Small-signal model – high frequency

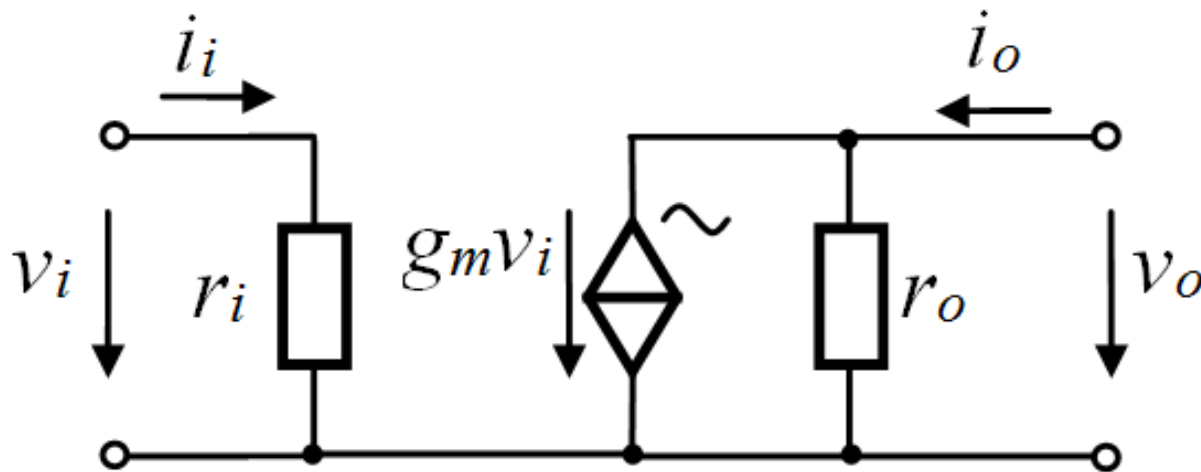


- two-port network

- ✓ r_i
- ✓ $g_m v_i$
- ✓ r_o

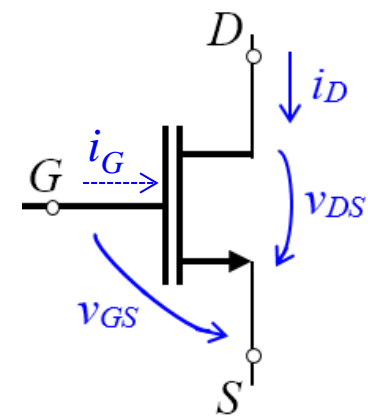
+ parasitic capacitances between terminals

➤ Small-signal model – low & medium frequency



Custom model for MOSFET?

- ✓ $r_i = ?$
- ✓ $g_m = ?, v_i = ?$
- ✓ $r_o = ?$



➤ Small-signal parameters

Input resistance r_i

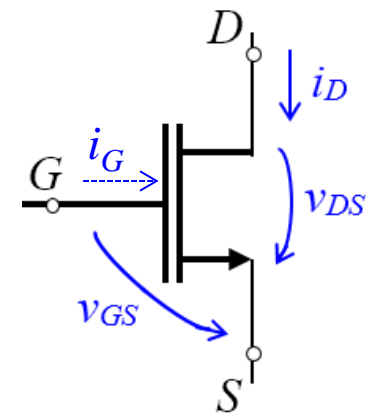
$$r_i = r_{gs} = \left. \frac{\partial v_{GS}}{\partial i_G} \right|_{v_{DS}=cst} = \left. \frac{v_{gs}}{i_g} \right|_{v_{DS}=cst}$$

$\frac{\partial v_{GS}}{\partial i_G}$ - derivative of v_{GS} with respect to i_G

the gate is electrically insulated from the rest of structure: $i_G = 0$

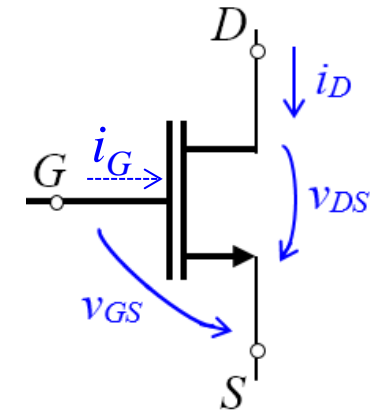
the input resistance is **infinite (open-circuit)**

$$r_{gs} = \infty$$



➤ Small-signal parameters

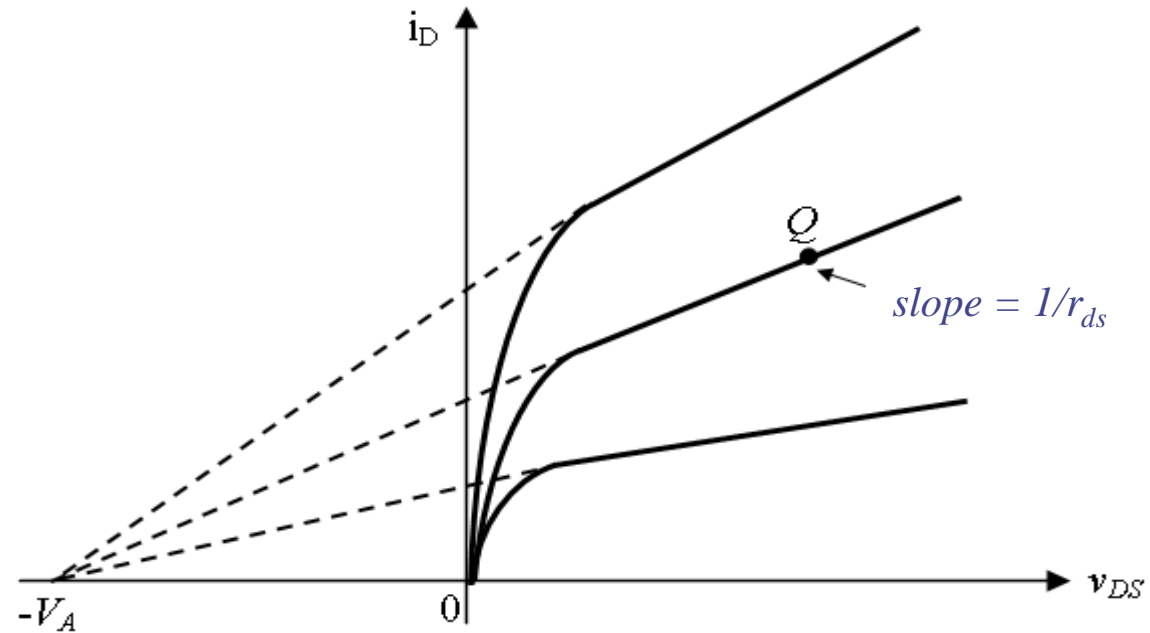
Output resistance r_o



$$r_o = r_{ds} = \frac{1}{g_o} = \left. \frac{\partial v_{DS}}{\partial i_D} \right|_{v_{GS} = cst} = \left. \frac{v_{ds}}{i_d} \right|_{v_{GS} = cst}$$

$\frac{\partial v_{DS}}{\partial i_D}$ - derivative of v_{DS} with respect to i_D

$$r_{ds} = \frac{V_A}{I_D}$$



$$i_D = \beta(v_{GS} - V_{Th})^2 \left(1 + \frac{v_{DS}}{V_A} \right)$$

V_A - Early voltage

$V_A = 100$ V for n-channel MOSFET

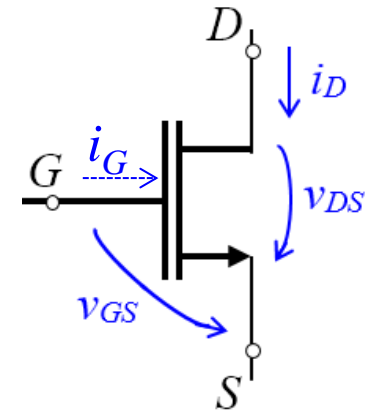
$V_A = 50$ V for p-channel MOSFET

$V_A = \frac{1}{\lambda}$, λ - channel length modulation factor [V^{-1}]

➤ Small-signal parameters

Transconductance g_m

- shows the transfer from variable input voltage v_{GS} to variable output current i_D



$$g_m = \left. \frac{\partial i_D}{\partial v_{GS}} \right|_{v_{DS} = cst} = \left. \frac{i_d}{v_{gs}} \right|_{v_{DS} = cst}$$

$$i_D = \beta (v_{GS} - V_{Th})^2$$

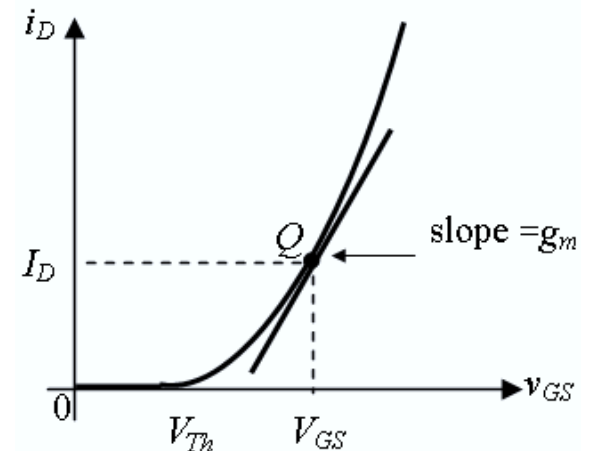
$$i_D = \frac{K W}{2 L} (v_{GS} - V_{Th})^2 \text{ - integrated transistors}$$

$$g_m = \frac{\partial (\beta (v_{GS} - V_{Th})^2)}{\partial v_{GS}} = 2\beta (V_{GS} - V_{Th})$$

$$g_m = 2\beta (V_{GS} - V_{Th}) = \frac{2I_D}{V_{GS} - V_{Th}} = 2\sqrt{\beta I_D}$$

integrated transistors:

$$g_m = 2 \sqrt{\frac{K W}{2 L} I_D}$$



MOSFET: voltage-controlled current source for small signal

$$i_d = g_m v_{gs}$$

➤ Small-signal model & parameters - **summary**

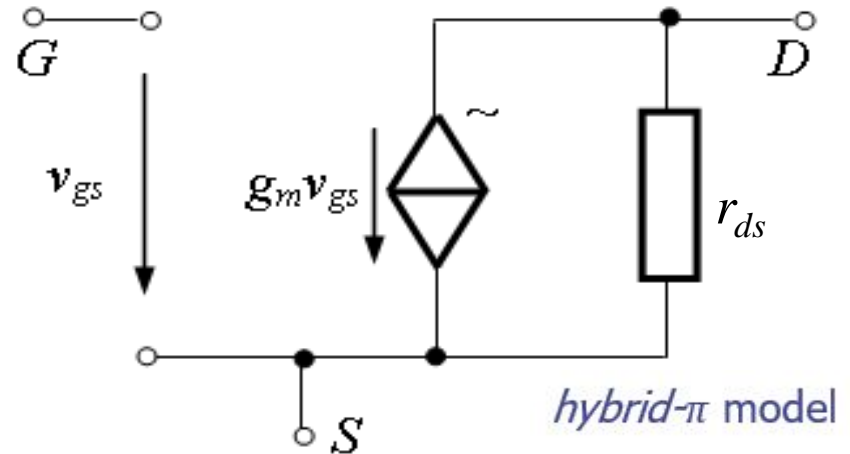
$$r_i = r_{gs} = \infty$$

$$g_m = 2\beta(V_{GS} - V_{Th}) = 2\sqrt{\beta I_D}$$

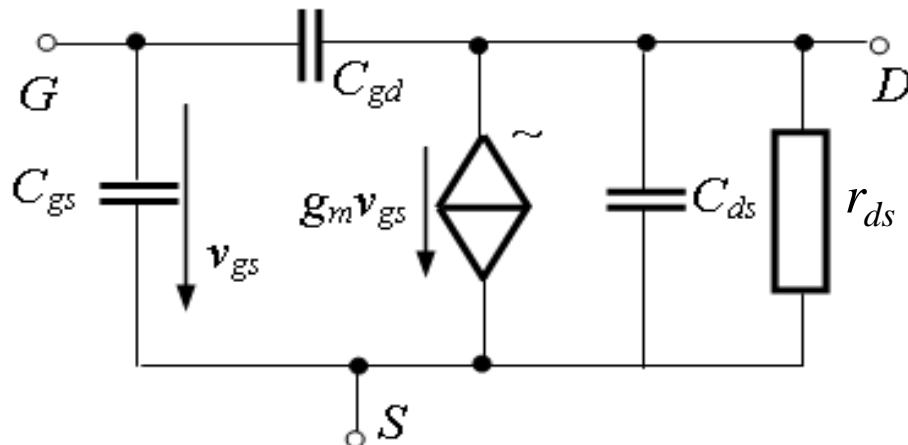
$$g_m = 2\sqrt{\frac{K}{2} \frac{W}{L} I_D}$$

$$r_o = r_{ds} = \frac{V_A}{I_D}$$

$$i_d = g_m v_{gs} = 2\beta(V_{GS} - V_{Th})v_{gs}$$



Small-signal model, **low & medium frequency**



Small-signal model, **high frequency**

Parasitic capacitances (pF or less) between terminals

➤ Small-signal model & parameters - examples

Ex. 1 $\beta = 2 \text{ mA/V}^2$, $V_A = 100 \text{ V}$; $I_D = 2 \text{ mA}$

$$g_m = 2\sqrt{\beta I_D} = 2\sqrt{2 \cdot 2} = 4 \text{ mS} \qquad r_{ds} = \frac{V_A}{I_D} = \frac{100}{2} = 50 \text{ K}\Omega$$

Ex. 2 $\beta = 2 \text{ mA/V}^2$, $V_{Th} = 1.5 \text{ V}$, $V_A = 100 \text{ V}$; $V_{GS} = 2.5 \text{ V}$

$$g_m = 2\beta(V_{GS} - V_{Th}) = 2 \cdot 2(2.5 - 1.5) = 4 \text{ mS}$$

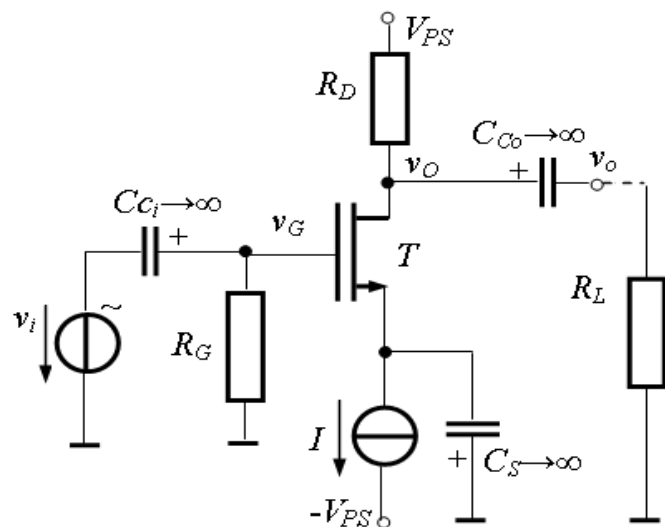
$$I_D = \beta(V_{GS} - V_{Th})^2 = 2(2.5 - 1.5)^2 = 2 \text{ mA} \qquad r_{ds} = \frac{V_A}{I_D} = \frac{100}{2} = 50 \text{ K}\Omega$$

Ex. 3 $K = 100 \text{ }\mu\text{A/V}^2$, $W/L = 1$, $V_A = 100 \text{ V}$; $I_D = 100 \text{ }\mu\text{A}$

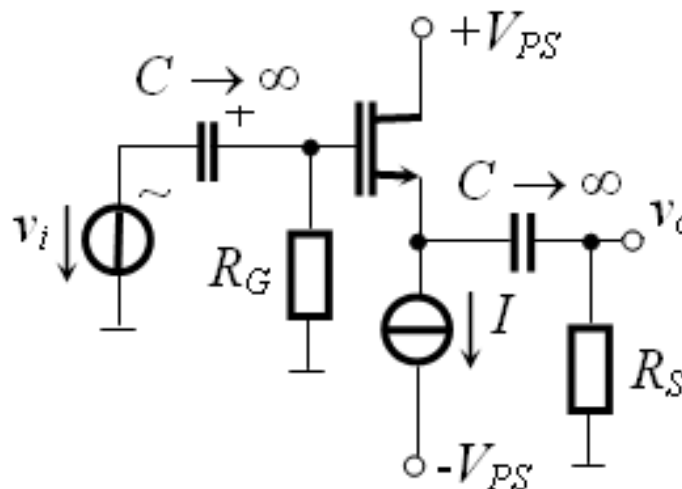
$$g_m = \sqrt{2K} \sqrt{\frac{W}{L}} \sqrt{I_D} = \sqrt{2 \cdot 100} \cdot \sqrt{1} \cdot \sqrt{100} = 0.14 \text{ mS}$$

$$r_{ds} = \frac{V_A}{I_D} = \frac{100}{0.1} = 1 \text{ M}\Omega$$

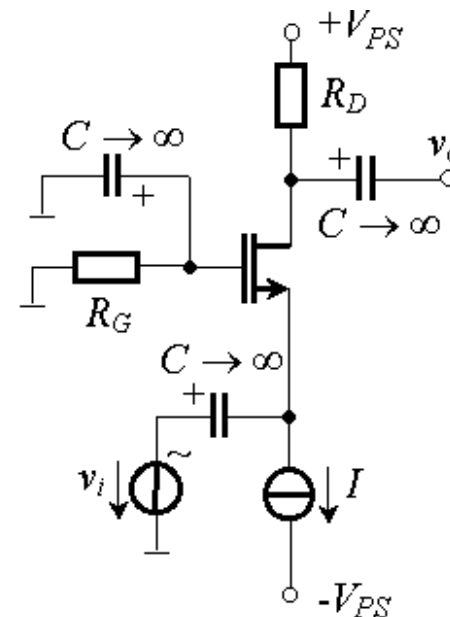
➤ Configurations



Common source (CS)



Common drain (CD)



Common gate (CG)

Where do the names of the configurations come from?

Why are the capacitors necessary?

How are the circuits analyzed?

➤ Configurations

- Where do the names of the configurations come from?

The terminal that is connected to **ground** in the **small-signal equivalent schematic** gives the name of the configuration.

- Why are the capacitors necessary?

Capacitors separate the variable signals from the dc ones (at the input, output, or in other points of the circuit).

The capacitances need to be **high enough** so that they can be considered **short circuits** at the operating frequency (their equivalent impedance \ll the series/parallel resistances connected with them).

On the **dc equivalent schematic** (the one used to determine the operating point Q), the capacitors are considered **open circuits**.

- How are the circuits analyzed?

See next slide(s)

➤ Transistor amplifier analysis - steps

Start with full amplifier circuit (transistor, resistors, capacitors, dc sources, ac sources)

1. Draw dc equivalent circuit

- compute the operating point $Q(V_{DS}; I_D)$
- determine dc potentials in the three terminals of the transistor
- compute small-signal parameters of the transistor: g_m , r_{ds}

C – open-circuit

2. Draw small-signal equivalent circuit

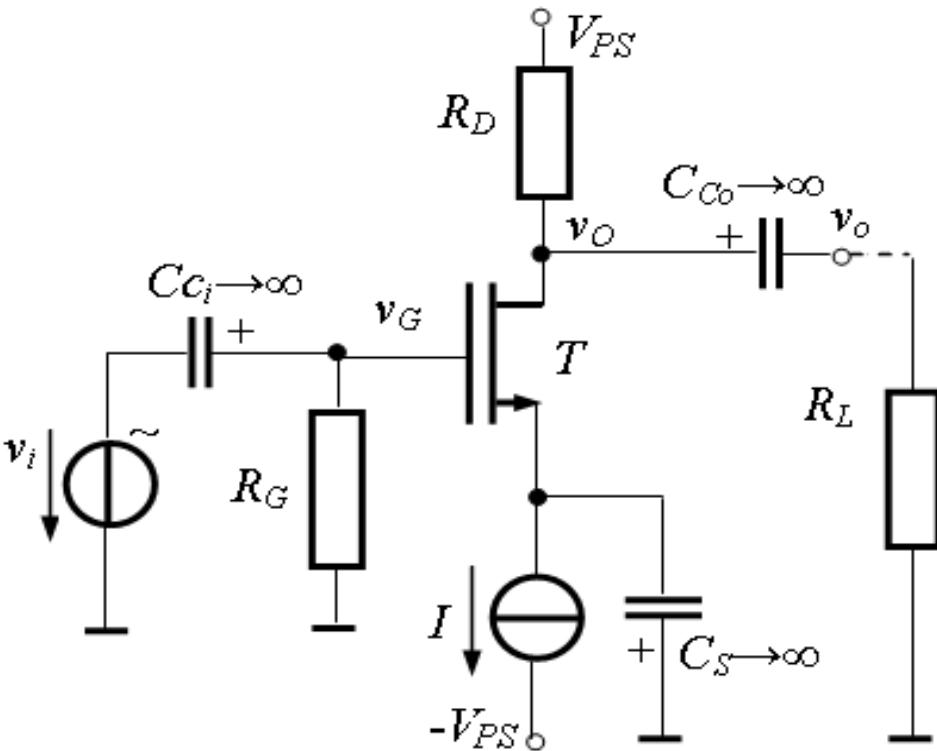
- compute amplifier performance: gain A_v
input resistance R_i , output resistance R_o

C – short-circuit
dc sources - passive

3. Plot waveforms in various points of the amplifier

- small-signal waveforms
- full waveforms (dc + small-signal)

➤ Common source (CS) basic amplifier



1. Draw dc equivalent circuit

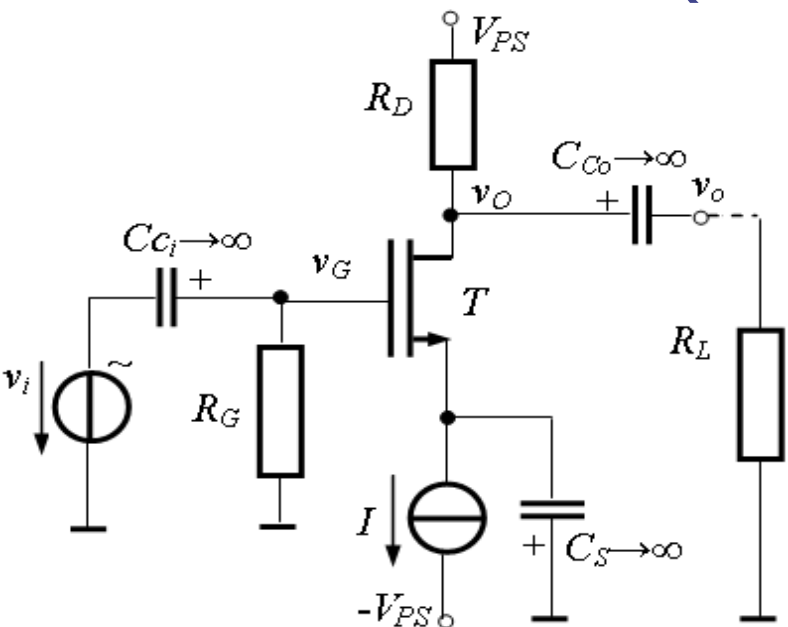
- compute the operating point $Q(V_{DS}; I_D)$
- determine dc potentials in the three terminals of the transistor
- compute small-signal parameters of the transistor: g_m, r_{ds}

See Seminar 1 and C2

$$g_m = 2\sqrt{\beta I_D}$$

$$r_{ds} = \frac{V_A}{I_D}$$

➤ Common source (CS) basic amplifier



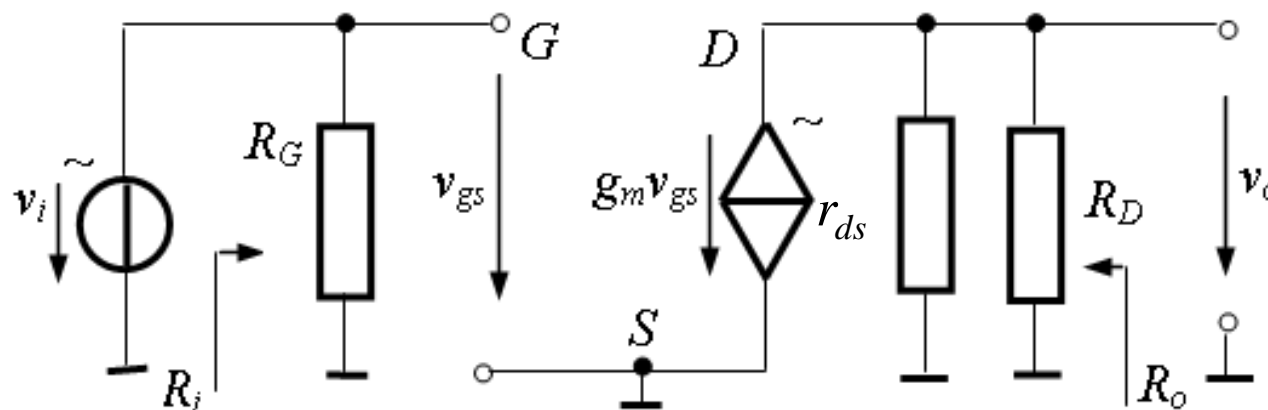
2. Draw small-signal equivalent circuit

- compute amplifier performance:

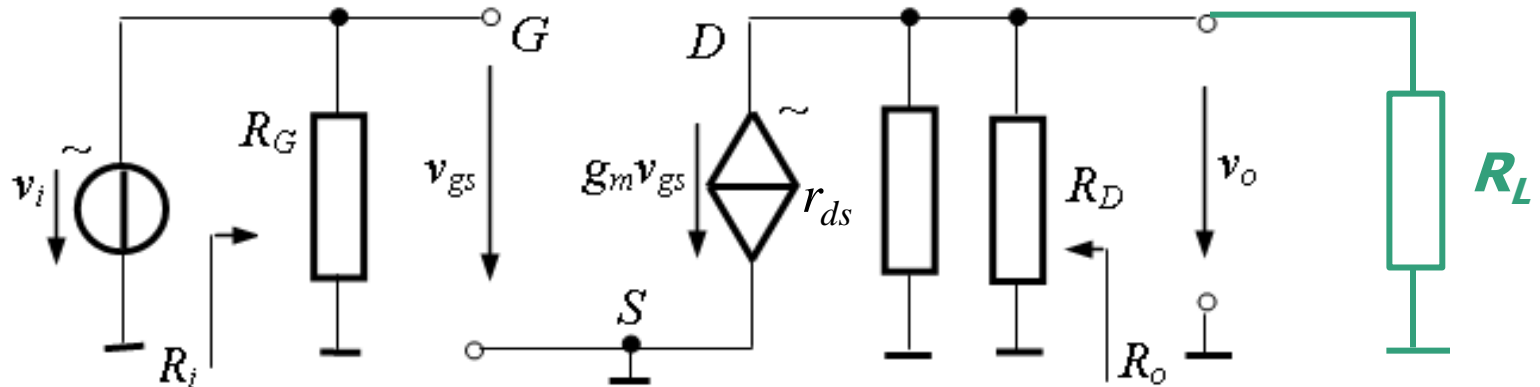
gain A_v

input resistance R_i

output resistance R_o



➤ Common source (CS) basic amplifier



$$R_i = R_G$$

Usually, $R_D \ll r_{ds}$, so $A_v \approx -g_m R_D$

$$A_v = \frac{v_o}{v_i}$$

$$R_o = R_D || r_{ds} \approx R_D$$

$$v_i = v_{gs}$$

$A_v < 0$ – inverting amplifier

$$v_o = -g_m v_{gs} (R_D || r_{ds})$$

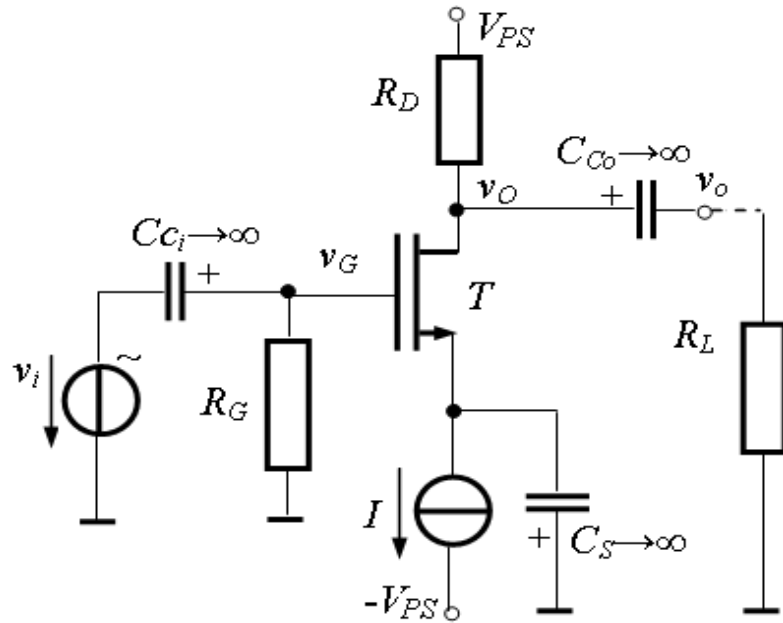
If R_L is present:

$$A_v = -g_m (R_D || r_{ds} || R_L)$$

$$A_v \approx -g_m (R_D || R_L)$$

$$A_v = -g_m (R_D || r_{ds})$$

➤ Common source (CS) basic amplifier - **example**



$$R_G = 1 \text{ M}\Omega; R_D = 50 \text{ K}\Omega;$$

$$I = 0.1 \text{ mA}; V_{PS} = 12 \text{ V}$$

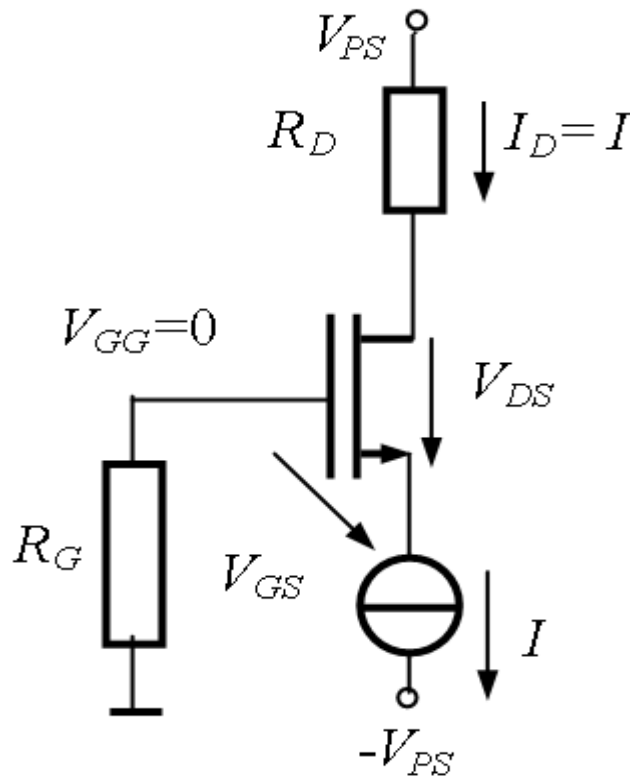
$$K = 0.1 \text{ mA/V}^2, W/L = 2, V_{Th} = 0.6 \text{ V}$$

$$V_A = 100 \text{ V}$$

- Draw the dc equivalent circuit.
- Determine $Q(V_{DS}, I_D)$.
- Compute the small-signal parameters of the transistor, g_m and r_{ds} .
- Draw the small-signal equivalent circuit. What is the configuration of the stage? Justify.
- Compute the gain, input and output resistances.
- For $v_i(t)$ - triangular wave, 50 mV amplitude, plot $v_G(t)$, $v_O(t)$, $v_{\alpha}(t)$, $v_S(t)$.

➤ Common source (CS) basic amplifier - **example**

- a) Draw the dc equivalent circuit.
- b) Determine $Q(V_{DS}, I_D)$.
- c) Compute g_m and r_{ds} .



$$I_D = I = 0.1 \text{ mA} \quad V_{GG} = 0\text{V}$$

$$V_{PS} = R_D I_D + V_{DS} - V_{GS} + V_{GG}$$

$$V_{DS} = V_{PS} - R_D I_D + V_{GS} - V_{GG}$$

$$I_D = \frac{k W}{2 L} (V_{GS} - V_{Th})^2$$

$$V_{GS} = V_{Th} + \sqrt{\frac{I_D}{\frac{k W}{2 L}}} = 0.6 + \sqrt{\frac{0.1}{\frac{0.1}{2} \cdot 2}} = 1.6 \text{ V}$$

$$V_{DS} = 12 - 50 \cdot 0.1 + 1.6 - 0 = 8.6 \text{ V}$$

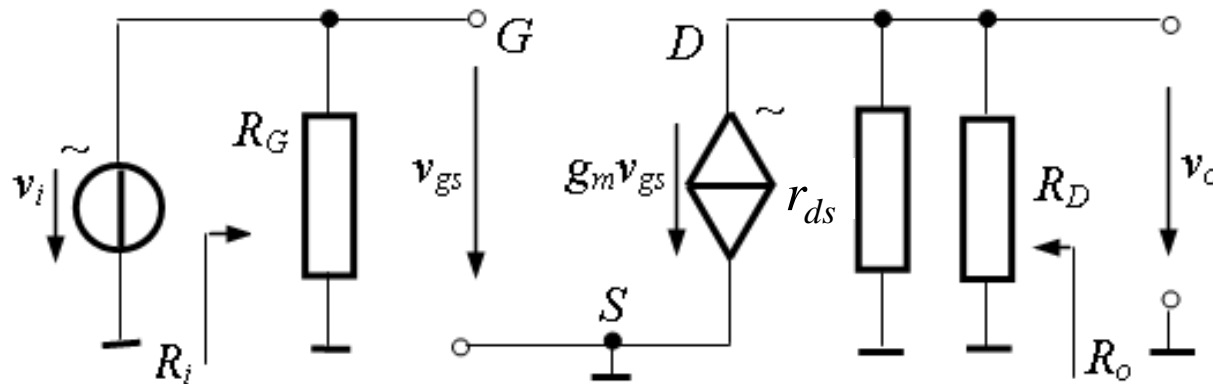
$Q(8.6 \text{ V}; 0.1 \text{ mA})$

$$g_m = \sqrt{2K} \sqrt{\frac{W}{L}} \sqrt{I_D} = \sqrt{2 \cdot 0.1} \cdot \sqrt{2} \cdot \sqrt{0.1} = 0.2 \text{ mS}$$

$$r_{ds} = \frac{V_A}{I_D} = \frac{100}{0.1} = 1\text{M}\Omega$$

➤ Common source (CS) basic amplifier - example

- d) Draw the small-signal equivalent circuit. What is the configuration of the stage? Justify.
 e) Compute the gain, input and output resistances.



common source, terminal S is connected to ground

$$A_v = -g_m(R_D || r_{ds}) = -0.2 \cdot (50 || 1000) = -9.5$$

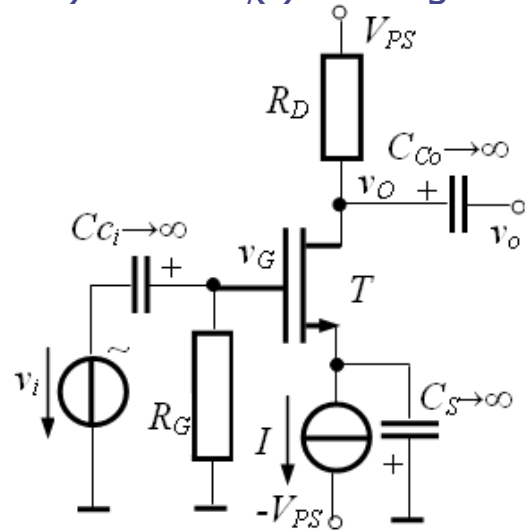
$$\text{or } A_v \approx -g_m R_D = -0.2 \cdot 50 = -10$$

$$R_i = R_G = 1 \text{ M}\Omega$$

$$R_o = R_D || r_{ds} = 47.6 \text{ K}\Omega \quad \text{or } R_o \approx R_D = 50 \text{ K}\Omega$$

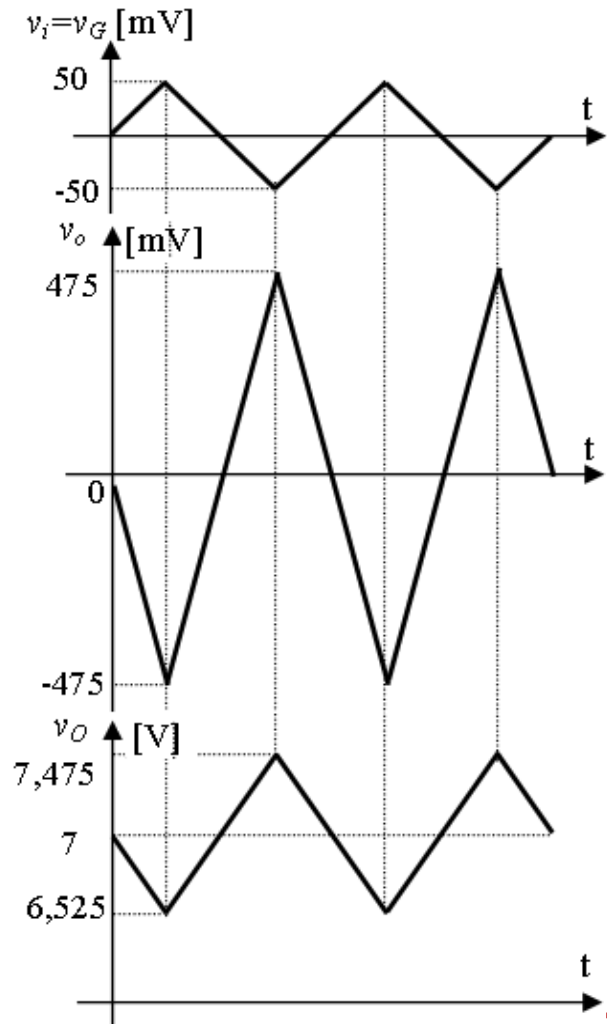
➤ Common source (CS) basic amplifier - **example**

f) For $v_i(t)$ - triangular wave, 50 mV amplitude, plot $v_G(t)$, $v_D(t)$, $v_S(t)$.



$$v_G(t) = V_G + v_i(t) \quad V_G = 0 \text{ V}$$

$$V_O = V_{PS} - R_D I = 7 \text{ V}$$



$$\widehat{V}_o = |A_v| \widehat{V}_i = 9.5 * 50 = 475 \text{ mV}$$

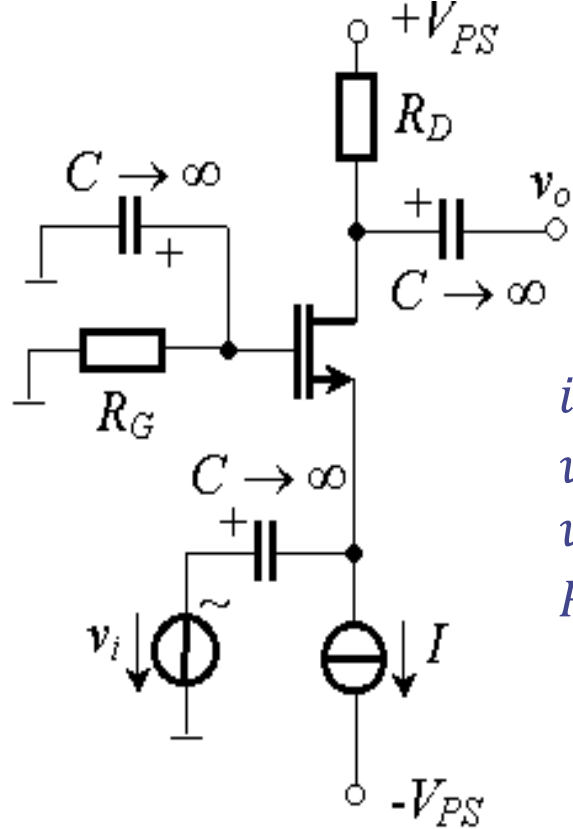
$$v_o(t) = A_v v_i(t) = -9.5 v_i(t)$$

$$v_o(t) = V_O + v_o(t) = 7 - 9.5 v_i(t)$$

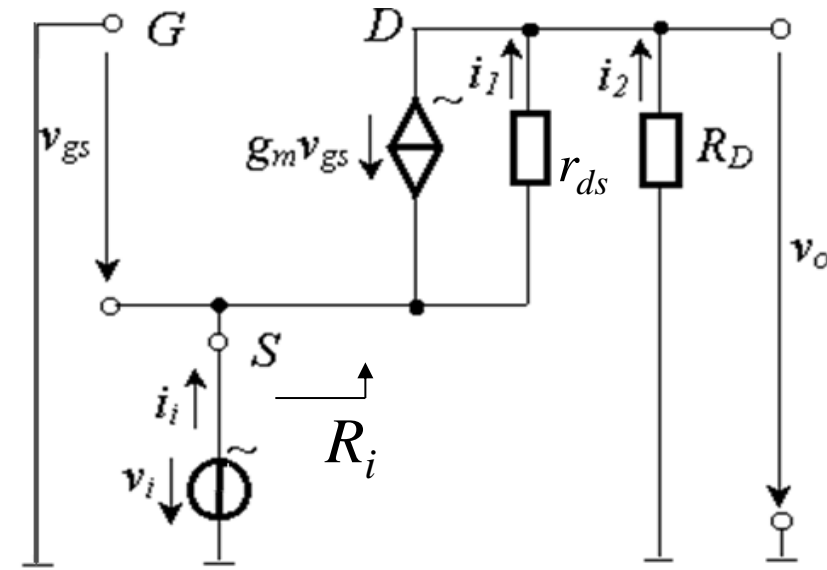
$$V_S = -V_{GS} + V_G = -1.6 \text{ V} \quad v_S(t) = 0 \text{ V}$$

$$v_S(t) = V_S + v_S(t) = -1.6 \text{ V}$$

➤ Common gate (CG) basic amplifier



$$\begin{aligned}
 i_1 &= g_m v_{gs} - i_2 \\
 v_o &= -R_D i_2 \\
 v_i &= -v_{gs} \\
 R_D i_2 - i_1 r_{ds} + v_i &= 0
 \end{aligned}$$



$$\begin{aligned}
 i_i &\approx -g_m v_{gs} \\
 v_i &= -v_{gs}
 \end{aligned}$$

$$R_i = \frac{v_i}{i_i} \approx \frac{1}{g_m}$$

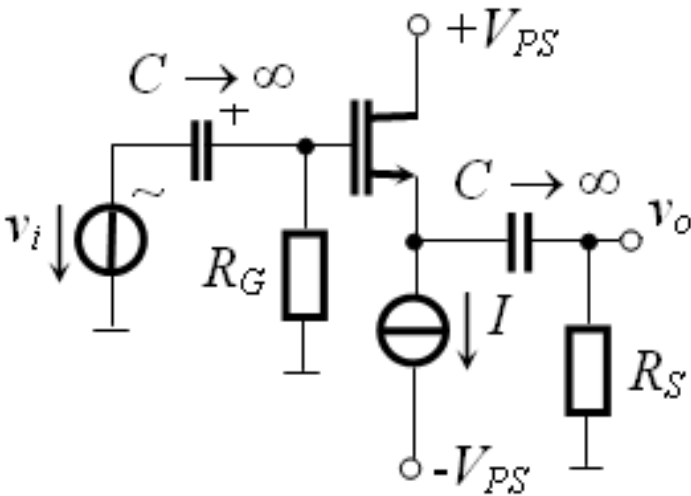
$$A_v = \frac{R_D (g_m r_{ds} + 1)}{R_D + r_{ds}}$$

If $g_m r_{ds} \gg 1$

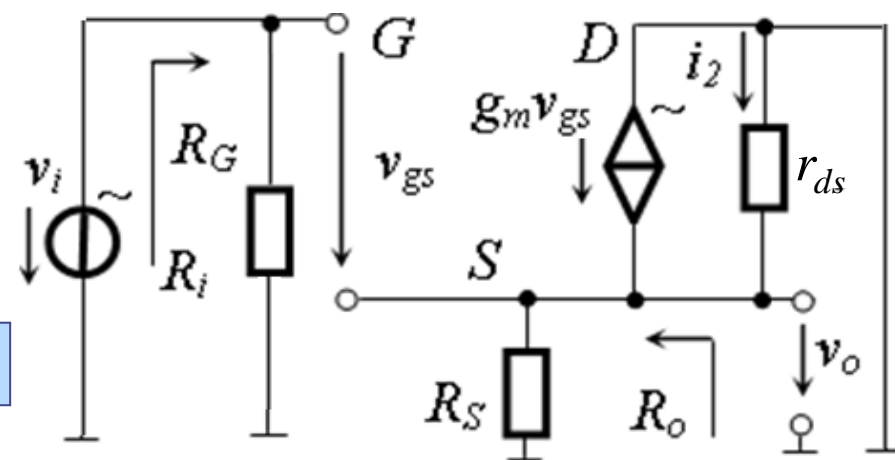
$$A_v \approx g_m (R_D \parallel r_{ds}) \approx g_m R_D$$

$$R_o = r_{ds} \parallel R_D \approx R_D$$

➤ Common drain (CD) basic amplifier



$$R_i = R_G$$



$$v_o = (R_S || r_{ds}) g_m v_{gs}$$

$$v_i = v_{gs} + v_o$$

$$A_v = \frac{v_o}{v_i} = \frac{(R_S || r_{ds}) g_m}{1 + (R_S || r_{ds}) g_m} \approx \frac{g_m R_S}{1 + g_m R_S}$$

If $g_m R_S \gg 1$

$$A_v \approx 1$$

Voltage follower (source follower)

r_s - resistance seen into S when $v_i = 0$

$$r_s = \frac{-v_{gs}}{-g_m v_{gs} - v_{gs}/r_{ds}} = \frac{1}{g_m + 1/r_{ds}} = r_{ds} || \frac{1}{g_m}$$

$$R_o = R_S || r_s = R_S || r_{ds} || \frac{1}{g_m} \approx R_S || \frac{1}{g_m}$$

➤ MOSFET basic amplifiers - summary

Common source CS

$$A_v = -g_m(R_D || r_{ds})$$

$$R_i = R_G$$

$$R_o = R_D || r_{ds} \approx R_D$$

Common gate CG

$$A_v \approx g_m(R_D || r_{ds}) \approx g_m R_D$$

$$R_i = \frac{v_i}{i_i} \approx \frac{1}{g_m}$$

$$R_o = r_{ds} || R_D \approx R_D$$

Common drain CD

$$A_v \approx 1$$

$$R_i = R_G$$

$$R_o \approx R_S || \frac{1}{g_m}$$

Which one is best? What does best mean for gain, input/output resistance?

Summary

- MOSFET small-signal model
- MOSFET basic amplifiers

Next week: BJT basic amplifiers.